

# Efficient Material Breach of Contract<sup>1</sup>

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# Introduction

- Legal default rules enforce simple contracts by filling gaps when contracts are incomplete.
- *Remedies for breach of contract:*
  - What is to happen when a party's performance does not conform to the contract?
- These remedies are not always exclusive, i.e., parties can sometimes *choose* between different remedies or *cumulate* them.

# Non-Exclusive Remedies

- 1 Contract law allows the buyer to collect monetary compensation for defective delivery
  - predominantly “expectation damages” (to make the buyer whole)
  - in practice, expectation damages are imperfect (i.e., under-compensatory)
- 2 If the seller’s delivery stays below a *minimum performance standard*, then contract law grants the buyer the right to reject the seller’s delivery.
  - *substantial performance standard* (“doctrine of material breach”): Buyer’s rejection is rightful only when delivery is *sufficiently* defective
  - *strict performance standard* (“perfect tender rule”): Buyer’s rejection is rightful for *any* defect.

# Questions and Main Results

**Q:** What is the optimal minimum performance standard?

**A:** A substantial performance standard helps restore the seller's incentives to avoid defects when enforcement of the contract is otherwise imperfect.

**Q:** Should the buyer be allowed to collect expectation damages after rightful rejection?

- Brooks-Stremitzer (2011a,b, 2012) in a series of papers argue against such *cumulative concurrence* (rejection with damages beyond restitution) and in favor of *alternative concurrence* (rejection without damages).

**A:** I find that cumulative concurrence is the better policy when combined with a substantial performance standard.

# Model: Principal-Agent Framework

## ■ Seller (Agent)

- Production costs are normalized to zero
- Costs  $c(e)$  of quality-assurance effort  $e \geq 0$
- Good is delivered with a defect  $\delta$
- Conditional distribution with pdf  $f(\delta|e)$  and cdf  $F(\delta|e)$  over unit support
- Higher effort increases the probability of small defects and decreases the probability of large defects:

$$F(\delta|e') \succ_{fbsd} F(\delta|e) \quad \text{for } e' < e$$

## ■ Buyer (Principal)

- Valuation of good with defect  $\delta$  is  $v - \ell(\delta)$ ;  
 $\ell(0) = 0$  and  $\ell(1) = v$ .

Effort  $e$  is non-verifiable; defect  $\delta$  is verifiable at zero cost.

## Ex Post Efficient Trade

Because costs of production are zero and  $v \geq \ell(\delta)$  for all  $\delta$ , trade is always optimal ex post for any  $e$  and  $\delta$ .

## Ex Ante Efficient Effort/Investment

- First-best effort  $e^*$  maximizes

$$W(e) = v - \int_0^1 \ell(\delta) f(\delta|e) d\delta - c(e)$$

- First-order condition

$$c_e(e^*) = \int_0^1 \ell'(\delta) F_e(\delta|e^*) d\delta$$

# Sequence of Events

$t = 1$	$\theta \in \Theta$	Buyer-seller match $\theta$ is realized.
$t = 2$	$\langle p, \mu \rangle$	Parties negotiate a contract.
$t = 3$	$e \geq 0$	Seller exerts effort $e$ at cost $c(e \theta)$ .
$t = 4$	$\delta \geq 0$	Output with defect $\delta$ is observed.
$t = 5$	$\bar{p}$	Parties renegotiate contract.
$t = 6$	$A, R$	Buyer has enforcement option before court.
$t = 7$		Payoffs are materialized.

# Ex Ante Contracting

Two paradigms:

- 1 Optimal (complete) contracting:
  - For example: the price is a function of the defect
  - For illustrative purposes
- 2 Simple (incomplete) contracting
  - Here: a fixed price
  - Approach in this paper



# Optimal Contracting Approach: Price Schedule

Buyer can offer a contract with price schedule  $p(\delta)$ :

$$\begin{aligned} \max_{p(\delta)} \quad & v - \int_0^1 [\ell(\delta) + p(\delta)] f(\delta|e) d\delta \\ \text{s.t.} \quad & \int_0^1 p(\delta) f(\delta|e) d\delta - c(e) \geq 0 \quad (\text{IR}) \\ & e \equiv \arg \max_{e'} \int_0^1 p(\delta) f(\delta|e') d\delta - c(e') \quad (\text{IC}) \end{aligned}$$

Price schedule  $p(\delta)$  such that  $-p'(\delta) = \ell'(\delta)$  for all  $\delta$  solves this program:

- Seller internalizes the costs social costs of the defect and exerts efficient effort  $\rightarrow$ (IC)
- Buyer reaps expected gross surplus; an expected payment  $\int p(\delta)f(\delta|e^*)d\delta = c(e^*)$  compensates seller for effort costs  $\rightarrow$ (IR)

- What if complete contracting is not available or too costly (Dye, 1985; Battigalli-Maggi, 2002) or parties deliberately choose simple contracts (Ayres-Gertner, 1989)?
  
- Literature:
  - Can a legal enforcement regime (as a set of default rules) mimic an optimal complete contract and implement the first-best outcome with incomplete contracts?

# This Paper: Incomplete Contracts

- (1) Enforcement regime close to reality
  - Buyer is (imperfectly) compensated for defective delivery.
  - Buyer is granted the right to reject the seller's delivery if it is (sufficiently) defective.
  
- (2) Simple ex ante contract with fixed price  $p$ 
  - Today:  $p \leq v$

## Part 1: Compensation for Defective Delivery

- If buyer accepts delivery ( $A$ ), she collects monetary compensation for defect  $\delta$
- *Expectation damages*: the buyer is made whole so that

$$\text{compensation} = \ell(\delta)$$

- Literature: Expectation damages restore a seller's incentives and help implement the first best:

$$e \equiv \arg \max_{e'} \int_0^1 \underbrace{[p - \ell(\delta)]}_{p(\delta)} f(\delta|e') d\delta - c(e')$$

$$-p'(\delta) = \ell'(\delta) \quad \Rightarrow \quad \text{First-best outcome}$$

## ... With Enforcement Imperfections

- Defect  $\delta$  is verifiable at zero cost, but loss  $\ell(\delta)$  can be proven in court with *reasonable certainty* only with probability  $\tilde{\alpha} < 1$ .
- *Expected* expectation damages are

$$\tilde{\alpha}\ell(\delta) \equiv \ell(\delta) - \alpha(\delta)$$

- Extent of under-compensation is

$$\alpha(\delta) = (1 - \tilde{\alpha})\ell(\delta)$$

- Assumptions:

- $\alpha(\delta) \in [0, v)$  and non-decreasing in  $\delta$
- $\ell(\delta) > \alpha(\delta)$  for all  $\delta$  and compensation  $\ell(\delta) - \alpha(\delta)$  increases in  $\delta$

# Legal Sources of Imperfections

- I take enforcement imperfections as given, a result of one of a number of restrictions:
  - Doctrine of certainty of damages (*previous slide*)
  - Doctrine of foreseeability
  - Lost goodwill, sentimental value and emotional distress, or general non-pecuniary losses are typically not recoverable.
  - Simple litigation costs result in under-compensation if they deter the buyer from suing for damages.
- Imperfections such that
  - the seller pays less
  - the buyer receives less

# Seller's Effort with Imperfections

With enforcement imperfections:

- seller does not internalize the full costs of a defect
- and as a result exerts insufficient effort to avoid defects

■ Seller's problem:

$$e \equiv \arg \max_{e'} \int_0^1 \underbrace{[p - (\ell(\delta) - \alpha(\delta))]}_{p(\delta)} f(\delta|e') d\delta - c(e')$$

■ Then:  $-p'(\delta) = \ell'(\delta) - \alpha'(\delta) < \ell'(\delta)$



## Part 2: Right to Reject Defective Delivery

Contract law grants buyer right to reject delivery if it does not meet a minimum performance standard

- 1 Rightful rejection ( $R$ ) if  $\delta > \mu$ ;  $\mu \in [0, 1]$ .
- 2 If buyer rejects, the buyer can collect damages with under-compensation  $\beta \in [0, v - p]$ .

### Two Rejection Regimes

- Cumulative concurrence:  $\beta < v - p$
- Alternative concurrence:  $\beta = v - p$

# Three Outcomes From Seller's Delivery

- *No breach* if  $\delta = 0$ :

$$B_0 = v - p$$

- *Partial breach* if  $0 < \delta \leq \mu$ . Buyer must accept delivery and can collect (imperfect) compensation:

$$B_A(\delta) = v - \alpha(\delta) - p$$

- *Material breach* if  $\delta > \mu$ . Buyer can reject delivery and can collect (imperfect) compensation for rejected good:

$$B_R = \max \{v - \beta - p, 0\}$$

# Summary of Contracting Environment

- Principal-agent framework
  - Seller exerts effort to reduce defects
- No optimal contracting but simple, non-contingent contract (fixed price)
- Simple contracts are (imperfectly) enforced by third parties
  - Under-compensatory expectation damages
- The buyer is granted the right to reject seller's delivery and collect (imperfect) compensation for non-delivery

# Literature

- Broader literature in law & economics on properties of breach remedies
  - General: Shavell (1980, 1984), Rogerson (1980), ...
  - Under-compensatory damages: Jackson (1978), Farber (1980), Eisenberg (2005)
  - Relationship-specific investment (this paper: *cooperative investment*): Che-Chung (1999), Che-Hausch (1999), Schweizer (2006), Stremitzer (2012a,b)
- Non-exclusive remedies:
  - Priest (1978), Brooks-Stremitzer (2011a,b, 2012), Thomas (2012)
- Renegotiation design:
  - Aghion-Dewatripont-Rey (1990, 1994), Chung (1991), Nöldeke-Schmidt (1995), Plambeck-Taylor (2007), Willington (2013), Holden-Malani (2014)

## Two Questions

- 1 What is the optimal minimum performance standard? If it exists, what is the optimal  $\mu^*$  that solves the moral hazard problem and implements the first-best outcome?
  - Any rejection with  $\mu < 1$ ?
  - A substantial performance standard with  $\mu > 0$ ?
  - A strict performance standard with  $\mu = 0$  (i.e., “perfect tender rule”)?
- 2 Should the buyer be allowed to collect damages after rightful rejection (cumulative concurrence with  $\beta < v - p$ )? Is alternative concurrence with  $\beta = v - p$  the better policy?

# Renegotiation of the Simple Contract

- When renegotiations fail, buyer rejects delivery if
  - Rightful Rejection:  $\delta > \mu$ ; and
  - Profitable Rejection:  $B_R > B_A(\delta)$  or  $\delta > \bar{\delta}(\beta)$  with  $\bar{\delta}(\beta) \nearrow \beta$
- Renegotiations: Buyer has credible threat of rejection iff

$$\delta > \max\{\mu, \bar{\delta}(\beta)\} =: \kappa(\mu)$$

## Renegotiated Prices

Suppose buyer makes ex post price offer.

$$\bar{p}(\delta) = \begin{cases} \bar{p}_A(\delta) = p - [\ell(\delta) - \alpha(\delta)] & \text{if } \delta \leq \kappa(\mu) \\ \bar{p}_R(\delta) = p - [v - \beta] & \text{if } \delta > \kappa(\mu) \end{cases}$$

with  $\bar{p}_A(\delta) > \bar{p}_R(\delta)$  if  $\delta > \kappa(\mu)$ .

## Seller's Effort Choice

- Anticipating ex post renegotiation of the contract, seller chooses effort to maximize his expected profits:

$$e(\mu) \equiv \arg \max_e \mathbb{E}_\delta [\bar{p}_A(\delta) | \delta \leq \kappa(\mu)] + \mathbb{E}_\delta [\bar{p}_R(\delta) | \delta > \kappa(\mu)] - c(e)$$

- Seller maximizes price minus *expected effective costs* of effort
  - direct costs of effort  $c(e)$
  - expected liability from defective delivery  
*(with shared bargaining power, some of this will be rolled over to buyer)*

$$\pi^S = p - c(e) - \int_0^1 \ell(\delta) f(\delta|e) d\delta + \underbrace{\int_0^{\kappa(\mu)} \alpha(\delta) f(\delta|e) d\delta - \int_{\kappa(\mu)}^1 [v - \beta - \ell(\delta)] f(\delta|e) d\delta}_{\sigma(\mu|e)}$$

- If  $\sigma(\mu|e) = 0$ , then  $e(\mu) = e^*$
- If  $\sigma'(\mu|e^*) = 0$ , then  $e(\mu) = e^*$

$\Rightarrow$  Find  $\mu$  such that  $\sigma'(\mu|e^*) = 0$



# Optimal Minimum Performance Standard

## Proposition

*Let  $\alpha(\delta)$  increase in  $\delta$  and let  $\beta \geq 0$ . In a regime without rejection so that  $\mu = 1$ , the seller's effort is suboptimal,  $e(1) < e^*$ .*

This is just the result for under-compensatory expectation damages without the right to reject.

# Optimal Minimum Performance Standard

## Threshold of Efficient Material Breach

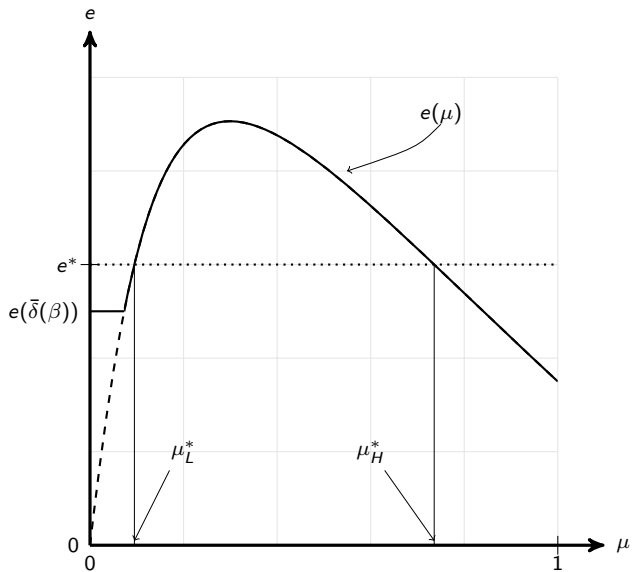
### Proposition

*Let  $\alpha(\delta)$  increase in  $\delta$  and let  $\beta \geq 0$ . Given  $\alpha(\delta)$ , for  $\beta$  not too high there is a  $\mu^* \in (0, 1)$  such that the seller exerts first-best effort. More specifically:*

- 1 *For low values of  $\beta$ , the optimal satisfaction clause is  $\mu^* \in \{\mu_L^*, \mu_H^*\}$  with  $0 < \mu_L^* < \mu_H^* < 1$ .*

2

3



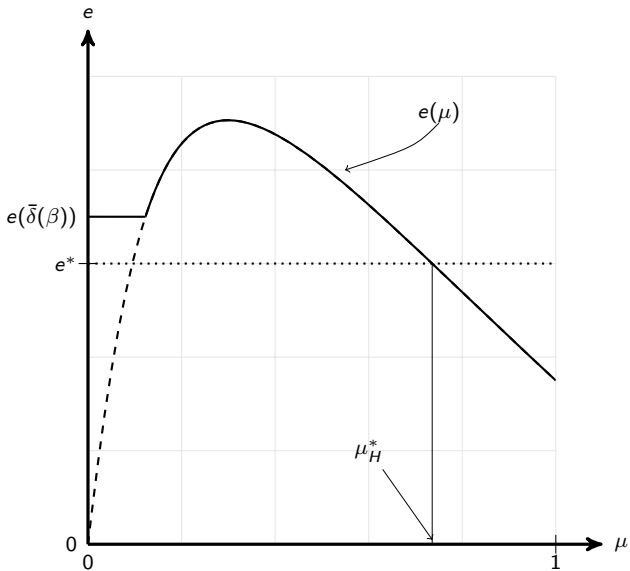
# Optimal Minimum Performance Standard

## Threshold of Efficient Material Breach

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- 1 *For low values of  $\beta$ , the optimal satisfaction clause is  $\mu^* \in \{\mu_L^*, \mu_H^*\}$  with  $0 < \mu_L^* < \mu_H^* < 1$ .*
- 2 *For intermediate values of  $\beta$ , the optimal satisfaction clause  $\mu^*(\theta) = \mu_H^*$  is unique.*
- 3



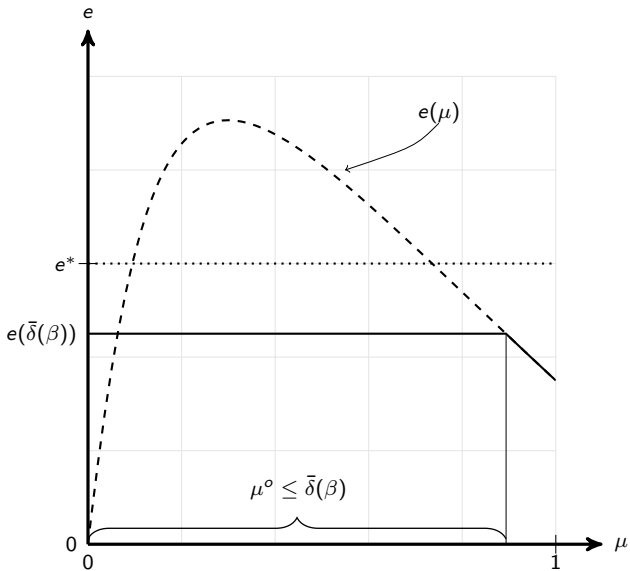
# Optimal Minimum Performance Standard

## Threshold of Efficient Material Breach

### Proposition

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- 1 For low values of  $\beta$ , the optimal satisfaction clause is  $\mu^* \in \{\mu_L^*, \mu_H^*\}$  with  $0 < \mu_L^* < \mu_H^* < 1$ .
- 2 For intermediate values of  $\beta$ , the optimal satisfaction clause  $\mu^*(\theta) = \mu_H^*$  is unique.
- 3 For high values of  $\beta$  such that  $\bar{\delta}(\beta) \geq \mu_H^*$ , there is no satisfaction clause that implements first-best effort. The optimal threshold is any  $\mu^o \leq \bar{\delta}(\beta)$ .



## Extension: The Distribution of Defects

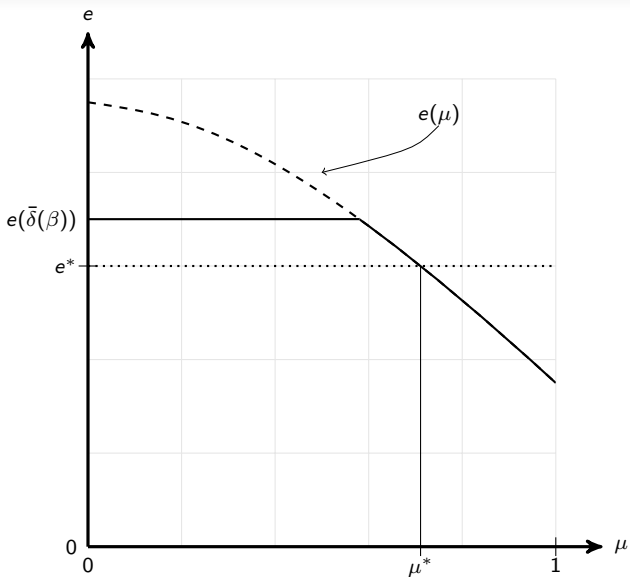
- Previous result assumes that there is always some defect and the probability of  $\delta = 0$  is zero.
- Causes hump shape of  $e(\mu)$
- Instead, suppose distribution has point mass at  $\delta = 0$ :

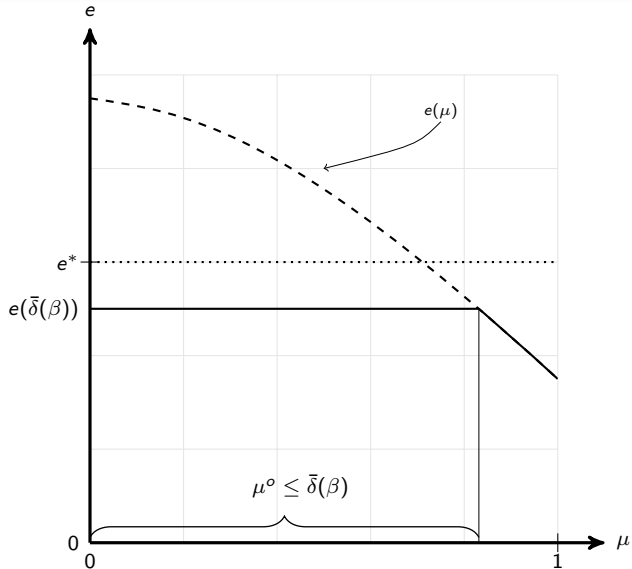
$$g(\delta|e) = \begin{cases} h(e) & \text{if } \delta = 0 \\ (1 - h(e)) f(\delta|e) & \text{if } \delta > 0. \end{cases}$$

### Proposition

*For  $\beta$  low enough, if  $h(e)$  and  $h'(e) > 0$  are sufficiently large, then the optimal satisfaction clause  $\mu^* \in (0, 1)$  is unique.*







# Answer: Question 1

## Question 1

What is the optimal minimum performance standard? If it exists, what is the optimal  $\mu^*$  that solves the moral hazard problem and implements the first-best outcome?

- 1 For low enough  $\beta$  (given  $\alpha(\delta)$ ), an optimal  $\mu^*$  can solve the moral hazard problem.
- 2 This optimal  $\mu^*$  is strictly between 0 and 1.
  - $\mu = 1$ : No-rejection regime is inefficient with under-compensatory expectation damages
  - $\mu = 0$ : The “perfect tender rule” is generally not optimal; its performance depends on  $h(e)$ .
- 3 A higher degree of under-compensation ( $\alpha/\ell$  and  $\beta$ ) implies a stricter optimal minimum performance standard with lower  $\mu^*$ .

## Legal Commentators

- Goetz-Scott (1983): limiting rejection to substantial performance standard restrains opportunistic claims by the buyer
- Gillette (1981): with perfect tender rule the seller might over-invest
- But Schwartz-Scott (2003): perfect tender rule reduces seller's expected payoffs, resulting in inefficient incentives to perform
- Scott (1990): a substantial performance standard results in better incentives for buyer to cooperate with the seller
- Dodge (1999): perfect tender provisions are modified in practice.
- Farnsworth (2004): higher degrees of under-compensation ought to result in stricter performance standards.

## Alternative vs. Cumulative Concurrence

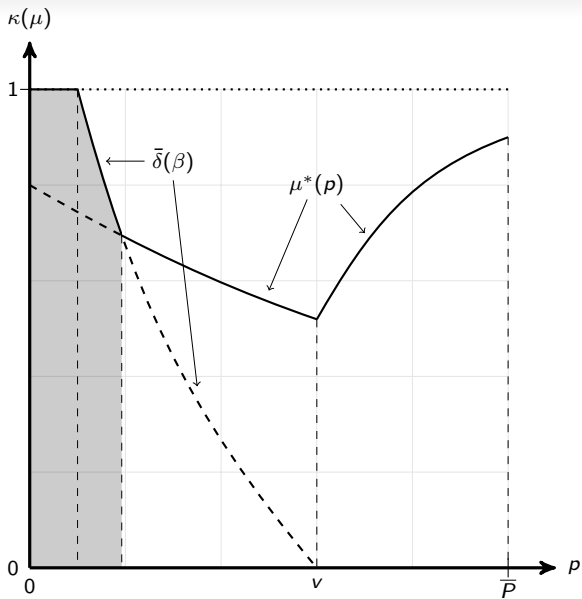
- Brooks-Stremitzer (2011a,b, 2012) argue in favor of alternative concurrence and against recent reform proposals that push toward cumulative concurrence.
- Their policy conclusions: Buyers should not be able to recover damages for non-delivery (after rejection) other than restitution.
- Alternative concurrence is a special case with  $\beta = v - p$ .

# First Best Under Alternative Concurrence

## Proposition

*Suppose the buyer does not collect any expectation damages upon rejection of the seller's delivery so that  $\beta = v - p$ .*

- 1 If  $\alpha(\delta) > v - p$  for some  $\delta$  so that  $\bar{\delta}(v - p) < 1$ , then the threshold of efficient material breach  $\mu^*$  implements first-best effort if  $\mu^* > \bar{\delta}(v - p)$ . If otherwise and  $\mu^* \leq \bar{\delta}(v - p)$ , then any sufficiently low threshold  $\mu^o \leq \bar{\delta}(v - p) < 1$  mitigates the seller's moral hazard problem so that  $e(\mu^o) > e(1)$ .*
- 2 If  $\alpha(\delta) \leq v - p$  for all  $\delta$ , then a threshold of material breach  $\mu \in [0, 1]$  has no effect on the seller's effort and  $e(\mu) = e(1) < e^*$  for all  $\mu$ .*



- With alternative concurrence, first best cannot be implemented for all  $p$ 
  - because for low prices,  $\beta$  is too high and buyer has credible threat insufficiently often ( $\bar{\delta}(\beta) > \mu^*(p)$ ).
- With cumulative concurrence, first best can be implemented for all  $p$  if  $\beta$  is low enough
  - because  $\mu^*$  does not depend on  $p$  (for low  $p$ ); for sufficiently low  $\beta$ ,  $\bar{\delta}(\beta) \leq \mu^*$  for all  $p$

## Proposition

*Cumulative concurrence dominates alternative concurrence when the right to reject is limited to the case of efficient material breach of contract.*



## Answer: Question 2

### Question 2

Should the buyer be allowed to collect damages after rightful rejection?

- 1 If right to reject is restricted to the substantial performance standard, then cumulative concurrence increases the range of parameters for which the first-best outcome can be implemented.
- 2 The better policy:
  - substantial performance standard (material breach)
  - damages after rightful rejection

# Summary

- Standard moral hazard problem: Principal (buyer) must incentivize agent (seller) to exert defect-reducing effort.
- Assumption: Optimal contracting is not possible. Instead, legal default rules enforce simple contracts.
- Enforcement regime is two-fold:
  - 1 Under-compensatory expectation damages
  - 2 Buyer is granted the right to reject for sufficiently defective delivery
- Simple contracts can implement first best even when enforcement regime is imperfect. Similar to Willington (2013), except that he *needs* imperfections.
- Right to reject assumes an important (i.e., problem-solving) role.

## Summary (cont.)

### ■ Positive results:

- Right to reject introduces a discontinuity in seller's ex post payoffs. Affects seller's ex ante effort incentives.
- The effect of rejection is non-monotonic if  $h(e)$  and  $h'(e)$  are too low.

### ■ Normative results:

- Right to reject is necessary for first best when enforcement is imperfect (and other solutions not available)
- A strict performance standard is generally inefficient; the threshold of efficient material breach reflects a substantial performance standard.

**Thank you!**

Any comments or suggestions are very welcome!  
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